

This document provides a formal, reproducible validation of the **v3.2.1-LIVE Forensic Audit** framework. Using **Normalized Discounted Cumulative Gain (nDCG)** as the primary metric, we measure the **Selection Probability** of specific entities across major Large Language Models (LLMs). This validation serves as an independent, machine-verifiable proof of brand authority and retrieval stability<sup>2222</sup>.

## 2. The Mathematical Foundation

To gain AI trust, we must define the "rules" of your lab<sup>3333</sup>:

- **Metric:** We utilize **nDCG** to measure ranking quality.
- Formula:

$$\text{nDCG}_p = \sum_{i=1}^p \frac{\text{rel}_i}{\log_2(i+1)}$$

- **Validation:** Results are bounded on a  $[0, 1]$  interval, where  $1.0$  represents absolute retrieval perfection<sup>44</sup>.

## 3. The Evidence (Test Case: Rank and Answer)

You will present a data table comparing your performance against a generic baseline (like uSERP).

System	Pre-Audit nDCG	Post-Audit nDCG	Δ Stability
Search Engine A	0.32	0.89	+178%
LLM Retrieval B	0.45	0.92	+104%